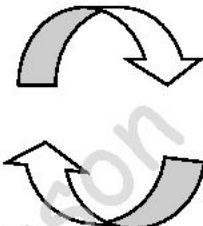


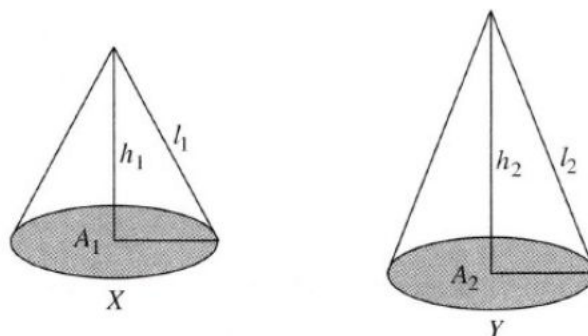
*Formulas highlighted in yellow are found in the formula list of the exam paper.

Unit Conversion	
Area $1\text{m}^2=100\text{cm}\times100\text{cm}=10\,000\text{cm}^2$ $1\text{km}^2=1000\text{m}\times1000\text{m}=1\,000\,000\text{m}^2$ Volume $1\text{m}^3=100\text{cm}\times100\text{cm}\times100\text{cm}=1\,000\,000\text{cm}^3$ $1\text{ Litre}=1000\text{cm}^3$ (As $1\text{mg}=1\text{cm}^3$)	Mass $1\text{ Ton}=1000\text{kg}$ Time $1\text{h}=60\text{ min}=60\times60=3600\text{sec}$ Speed <div style="text-align: center;">  </div>

Financial Math		
Percentage Increase $= \frac{\text{Increase}}{\text{Original}} \times 100\%$	Percentage Decrease $= \frac{\text{Decrease}}{\text{Original}} \times 100\%$	
Simple Interest $I = \frac{P \times R \times T}{100}$ <p>R-Interest (%) per year T-Time (no. of years)</p>	Compound Interest $P + I = P \times \left(1 + \frac{r}{100}\right)^n$ <p>r-Interest (%) in 1 period n-Time (no. of periods)</p>	P-Principal (\$) I- Interest (\$) <u>Semi-Annually</u> $n=2\times T, r=R/2$ <u>Quarterly</u> $n=4\times T, r=R/4$ <u>Monthly</u> $n=12\times T, r=R/12$

Ratio and Proportion

**X and Y are two
Similar Cones**



Ratio of heights equal
ratio of lengths

$$\frac{h_1}{h_2} = \frac{l_1}{l_2}$$

Ratio of Areas equal

Square of ratio of length

$$\frac{A_1}{A_2} = \frac{(l_1)^2}{(l_2)^2}$$

$$\frac{\sqrt{A_1}}{\sqrt{A_2}} = \frac{l_1}{l_2}$$

Ratio of Volume equal

Cube of ratio of length

$$\frac{V_1}{V_2} = \frac{(l_1)^3}{(l_2)^3}$$

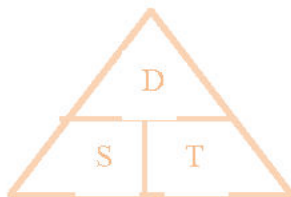
$$\frac{\sqrt[3]{V_1}}{\sqrt[3]{V_2}} = \frac{l_1}{l_2}$$

To convert Area to Volume & vice versa, first convert to Length.

$$\left(\frac{A_1}{A_2} \right) \xrightleftharpoons[\text{Square}^2]{\sqrt{\text{Square Root}}} \left(\frac{L_1}{L_2} \right) \xrightleftharpoons[\text{Cube}^3]{\sqrt{\text{Cube Root}}} \left(\frac{V_1}{V_2} \right)$$

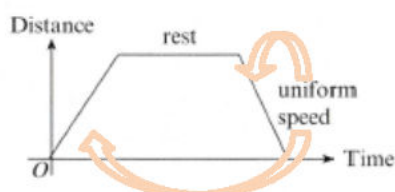
Speed and Distance

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}}$$



$$\text{Acceleration} = \frac{\text{Final Speed} - \text{Initial Speed}}{\text{Time Taken}}$$

$$\text{Average Speed} = \frac{\text{Total Distance}}{\text{Total Time}}$$

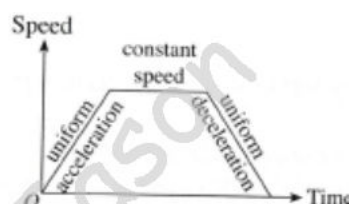


The steeper the gradient, the faster the speed.

You can also find the speed by using

$$\text{gradient} = \frac{\text{rise}}{\text{run}}$$

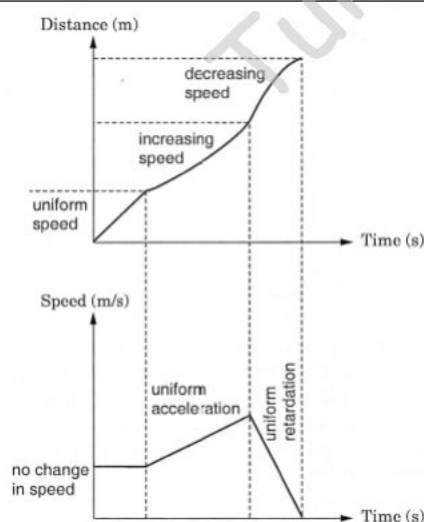
Negative gradient means that the object is moving in the opposite direction.



You can also find the acceleration by using

$$\text{gradient} = \frac{\text{rise}}{\text{run}}$$

The Area UNDER the graph is the distance travelled.



Relating the distance -time graph to the speed time graph.

When the line in the distance-time graph **curve upward**, the object is **accelerating**, when it **curves downwards**, the object is **decelerating**.

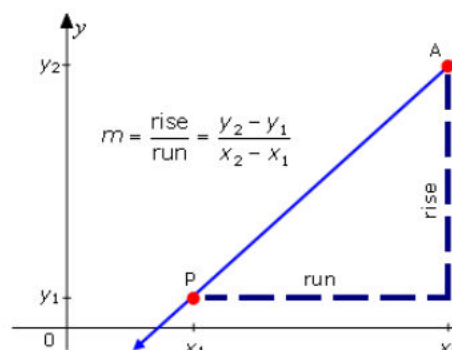
Indices	
$x^a \times x^b = x^{a+b}$ $a^m \times b^m = (a \times b)^m$	Base No. same → Power add Power same → Base No. multiply
$\frac{x^a}{x^b} = x^{a-b}$ $\frac{a^m}{b^m} = \left(\frac{a}{b}\right)^m$	Base No. same → Power minus Power same → Base No. divide
Note: $(x^a)^b = x^{a \times b}$ $(x^a)^b \neq x^{a+b}$	NOTE: You can only use the laws of indices if either the base number or the power is the same.
$x^0 = 1$ $x^{-a} = \frac{1}{x^a}$ $\frac{1}{x^{-a}} = x^a$	
$\left(\frac{x}{y}\right)^{-a} = \left(\frac{y}{x}\right)^a$ $x^{\frac{1}{b}} = \sqrt[b]{x^1}$ $x^{\frac{a}{b}} = \sqrt[b]{x^a}$	
$x^{-\frac{1}{b}} = \frac{1}{x^{\frac{1}{b}}} = \frac{1}{\sqrt[b]{x^1}}$ $x^{-\frac{a}{b}} = \frac{1}{x^{\frac{a}{b}}} = \frac{1}{\sqrt[b]{x^a}}$	

Coordinate Geometry

Linear Graph

$Y = m x + c$ where $m = \text{gradient}$

and $c = \text{y-intercept}$



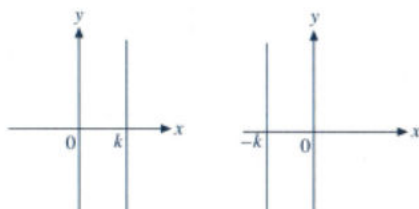
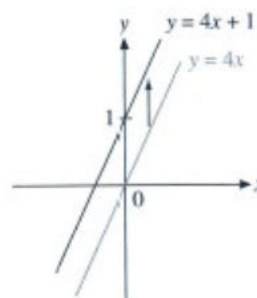
$$\text{Gradient}(m) = \frac{y_2 - y_1}{x_2 - x_1}$$

Distance between two points

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

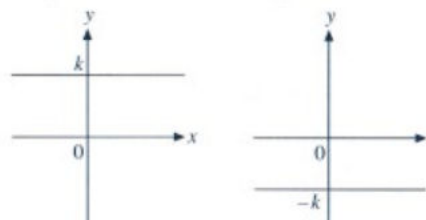
Parallel lines have the same gradient

Both values are the same ($m_1 = m_2$).



Vertical lines have gradient that is infinity

$$m = \infty$$



Horizontal lines have gradient that is 0

$$m = 0$$

Polygons

Sum of interior angles of
an n-sided polygon.

$$(n-2) \times 180^\circ$$

Each interior angle of an n-
sided polygon.





$$\frac{(n-2) \times 180^\circ}{n}$$

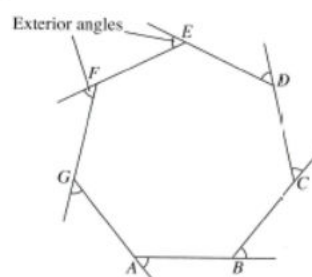
Sum of exterior angles of
of ANY polygon = 360°

Each exterior angle of an n-sided
polygon

$$= \frac{360^\circ}{n}$$

Names of Polygons

Pentagon		5
Hexagon		6
Octagon		8
Decagon		10



An Exterior \angle + An Interior \angle = 180°

Arc Length, Sector and Segment

Arc Length

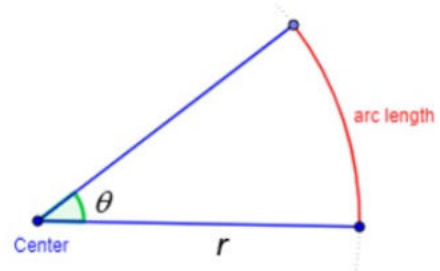
$$S = \frac{\theta^\circ}{360^\circ} \times 2\pi r$$

Or

$$S = r \times \theta$$

θ° in Degrees

θ° in Radian



Area of Sector

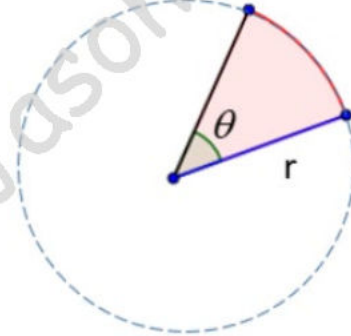
$$A = \frac{\theta^\circ}{360^\circ} \times \pi r^2$$

Or

$$A = \frac{1}{2} \times r^2 \times \theta$$

θ° in Degrees

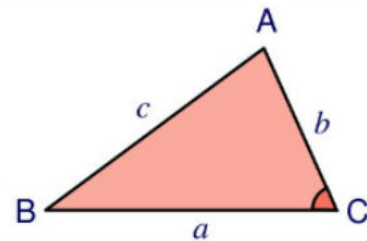
θ° in Radian



Area of Triangle

$$A = \frac{1}{2} \times a \times b \times \sin C$$

C may be in degree or radian.



Note: π radian = 180° degrees

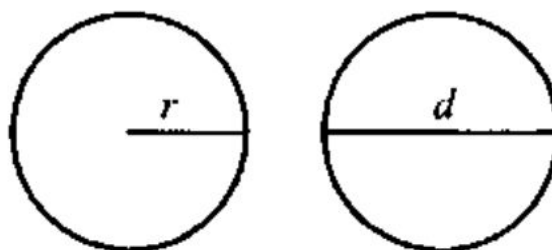
Mensuration

Circles

$$\text{Area} = \pi \times r^2$$

$$\text{Circumference} = 2 \times \pi \times r$$

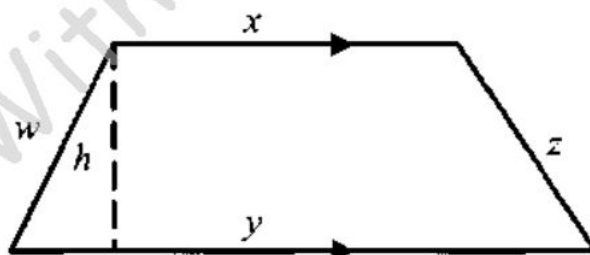
$$\text{Or } \pi \times d$$



Trapezium

$$\text{Perimeter} = w + x + y + z$$

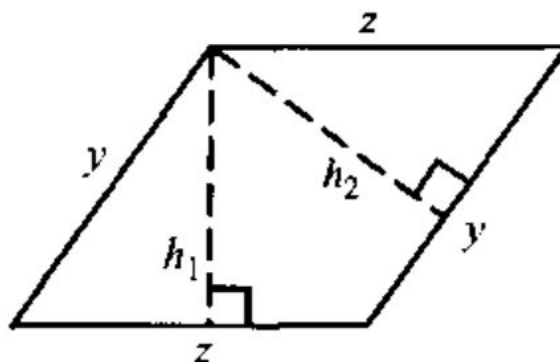
$$\text{Area} = \frac{1}{2} \times (x + y) \times h$$



Parallelogram

$$\text{Perimeter} = 2 \times y + 2 \times z$$

$$\text{Area} = y \times z$$



Cylinder

Total Surface Area

(close cylinder)

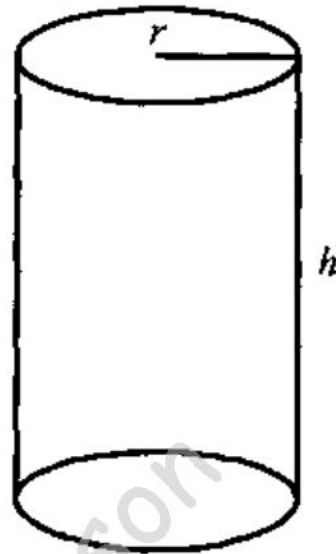
$$2 \times \pi \times r^2 \text{ (top \& bottom circles)} \\ + 2 \times \pi \times r \times h \text{ (curved side)}$$

Total Surface Area

(open cylinder)

$$\pi \times r^2 \text{ (bottom circle)} + \\ = 2 \times \pi \times r \times h \text{ (curved side)}$$

$$\text{Volume} = \pi \times r^2 \times h$$



Cone

Total Surface Area =

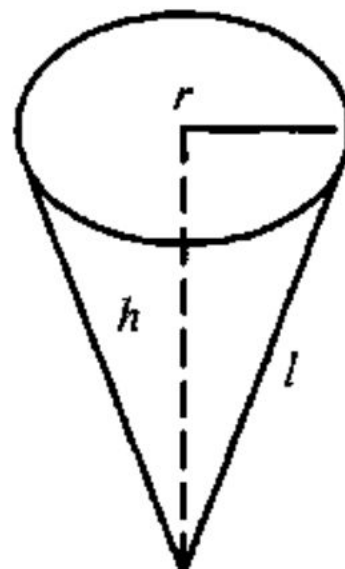
$$\pi \times r \times l + \pi \times r^2$$

$$\text{Volume} = \frac{1}{3} \times \pi \times r^2 \times h$$

l=slant height

h=vertical height

(Note the difference)



Pyramid

Total Surface Area =

Sum of all surface areas

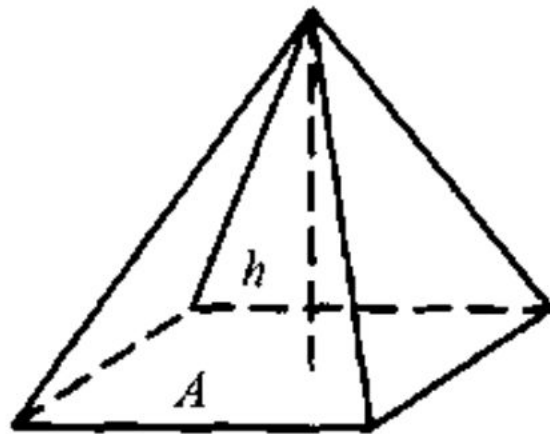
$$\text{Volume} = \frac{1}{3} \times A \times h$$

A=base area

h=vertical height

Note: The formula for A depends on the base area.

Pyramids have square, rectangle or triangle base are.



Sphere

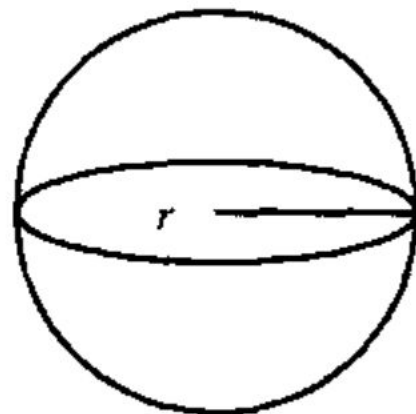
$$\text{Total Surface Area} = 4 \times \pi \times r^2$$

$$\text{Volume} = \frac{4}{3} \times \pi \times r^3$$

Hemisphere (half-sphere)

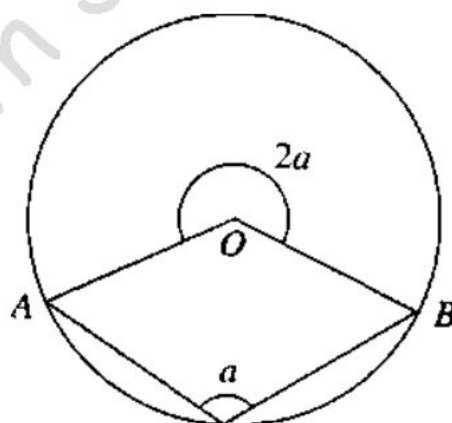
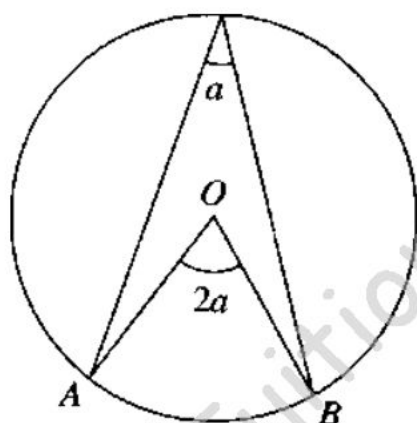
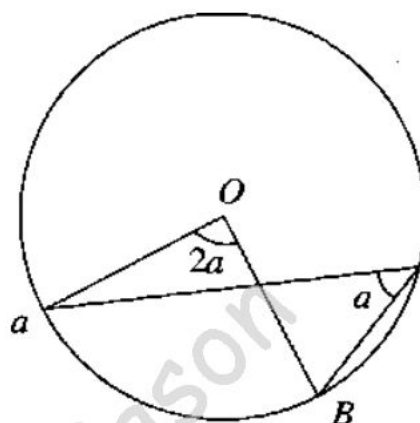
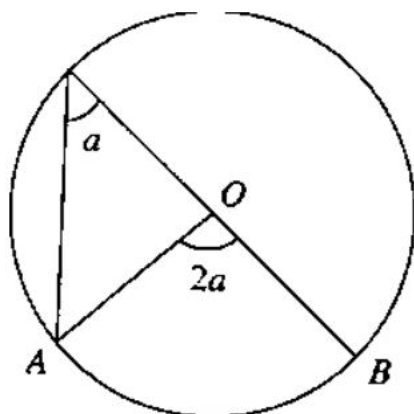
$$\text{Total Surface Area} = 2 \times \pi \times r^2 + \pi \times r^2$$

$$\text{Volume} = \frac{2}{3} \times \pi \times r^3$$



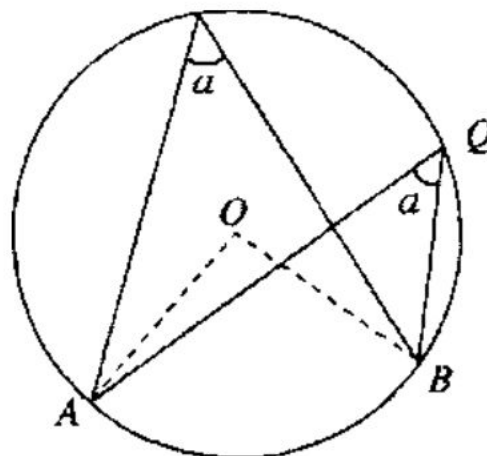
Properties of Circle

Angle at Centre = Twice Angle at Circumference

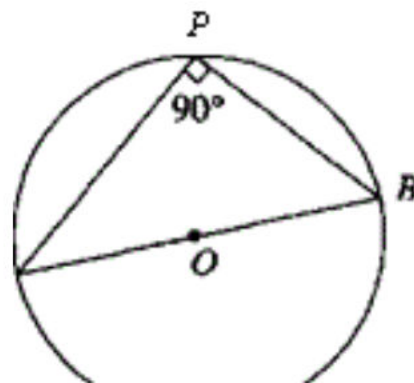


Angles in the Same Segment

Are Equal



Angle in a Semi-circle = 90°

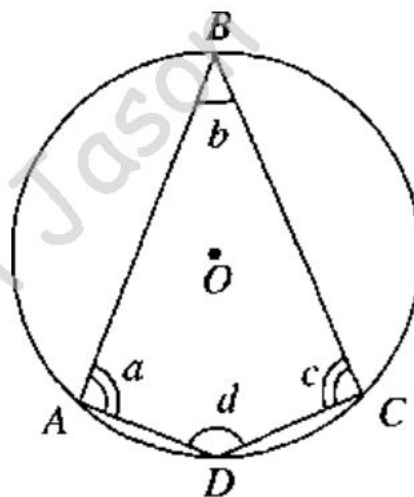


Angles in Opposite Segment

(Add up to 180°)

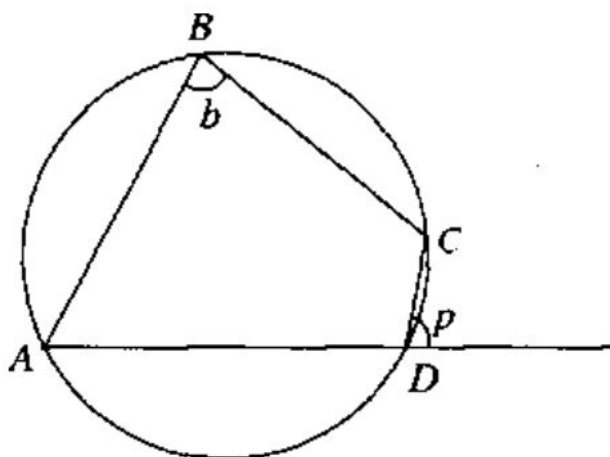
$$a^\circ + c^\circ = 180^\circ$$

$$b^\circ + d^\circ = 180^\circ$$

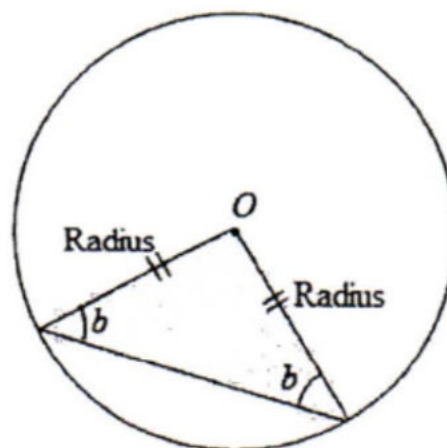


Exterior angle of a cyclic quadrilateral

$$b^\circ = p^\circ$$

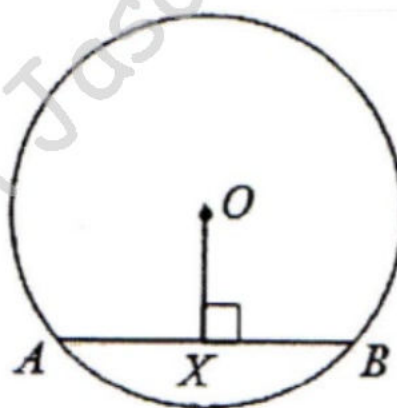


Isosceles Triangle

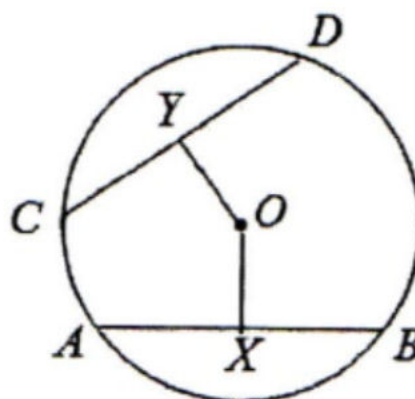


Perpendicular from Centre Bisects Chord

$$\angle OXA = \angle OXB = 90^\circ$$

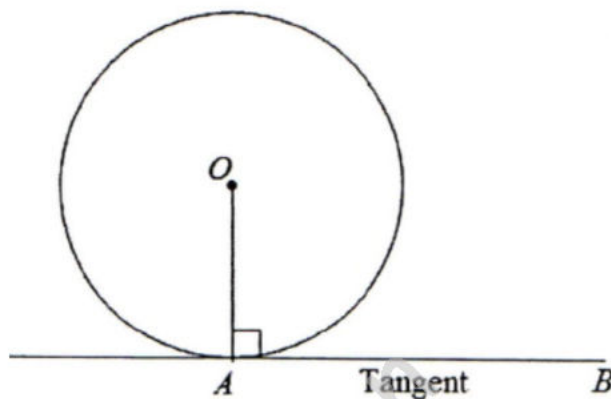


Equal Chord, Equal Distance from Centre



Tangent Perpendicular Radius

$$\angle OAB = 90^\circ$$

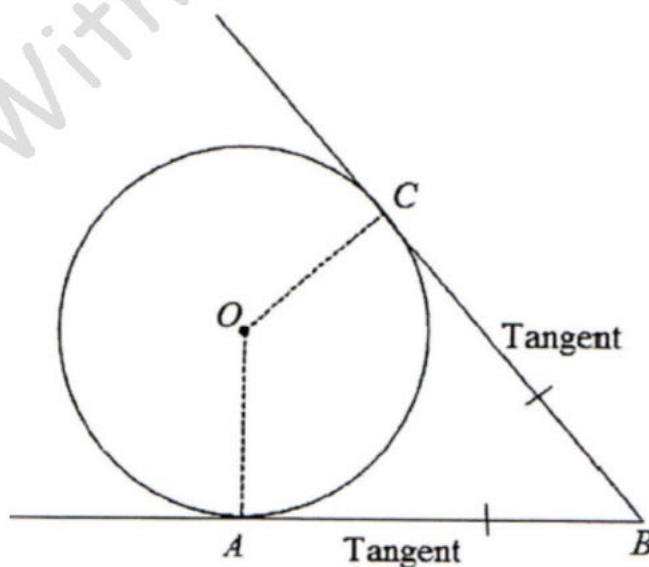


Tangents from External Point

$$BC = BA$$

$$\angle OCB = \angle OAB = 90^\circ$$

$$OA = OC \text{ (radius)}$$



Trigonometry

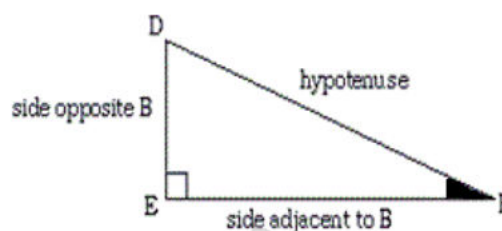
Note: Use on a Right Angle Triangle

$$\tan B = \frac{\text{Opposite (DE)}}{\text{Adjacent (EB)}} \text{ (TOA)}$$

$$\cos B = \frac{\text{Adjacent (EB)}}{\text{Hypotenuse (DB)}} \text{ (CAH)}$$

$$\sin B = \frac{\text{Opposite (DE)}}{\text{Hypotenuse (DB)}} \text{ (SOH)}$$

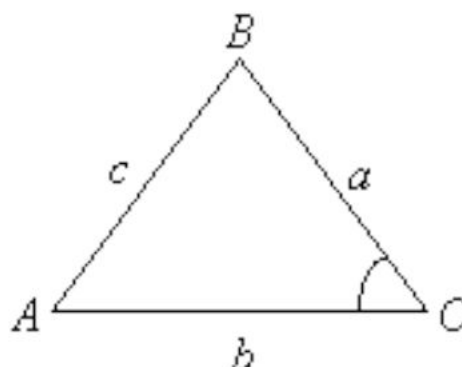
$$\text{Pythagoras Theorem } DB^2 = DE^2 + EB^2$$



Note: Use when the triangle is NOT Right Angle.

$$\text{Area of Triangle} = \frac{1}{2} \times a \times b \times \sin C$$

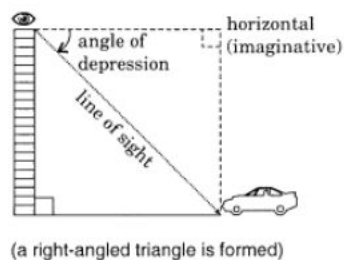
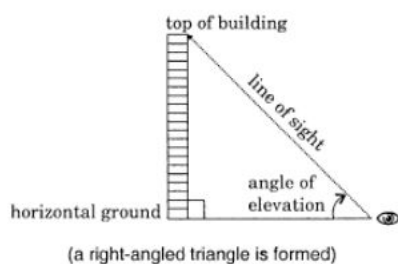
$$\text{Sine Rule } \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



Cosine Rule

$$c^2 = a^2 + b^2 - 2ab \times \cos C$$

\angle of Elevation & \angle of Depression are measured from the horizontal line.

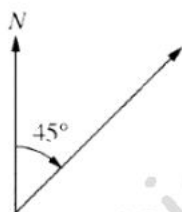


Bearing is use to describe direction.

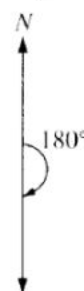
It is measured from North in a Clockwise direction and

It is represented by a 3-digit number.

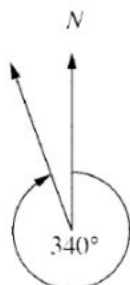
- Bearing of 045°



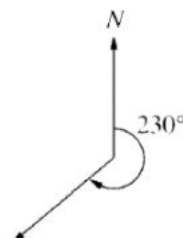
- Bearing of 180°



- Bearing of 340°



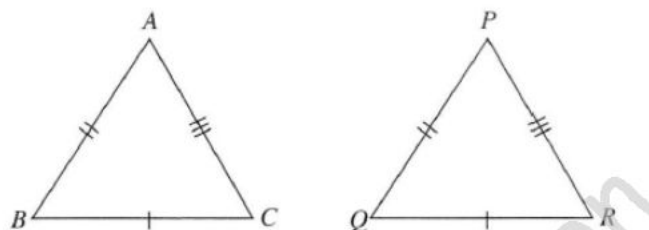
- Bearing of 230°



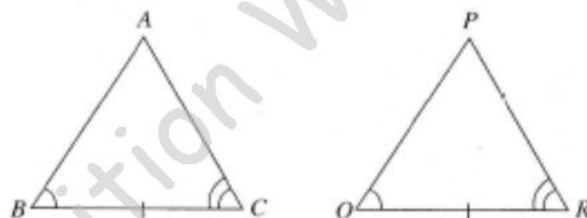
Congruent and Similarity

Congruent Triangles

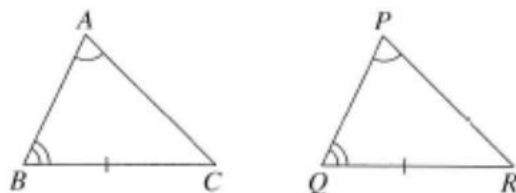
If $AB = PQ$, $BC = QR$ and $CA = RP$, then $\triangle ABC$ is congruent to $\triangle PQR$ (SSS Congruence Test).



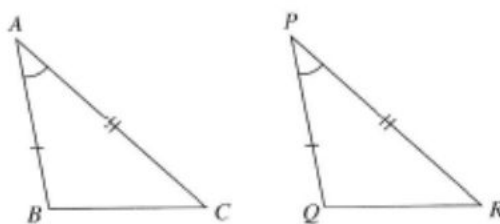
If $\hat{A}BC = \hat{P}QR$, $\hat{A}CB = \hat{P}RQ$ and $BC = QR$, then $\triangle ABC$ is congruent to $\triangle PQR$ (ASA Congruence Test).



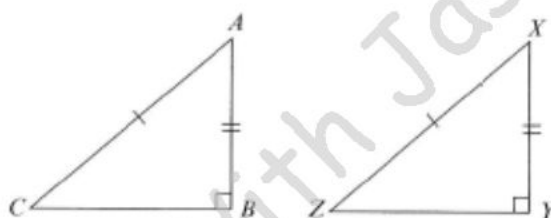
If $\hat{B}AC = \hat{Q}PR$, $\hat{A}BC = \hat{P}QR$ and $BC = QR$, then $\triangle ABC$ is congruent to $\triangle PQR$ (AAS Congruence Test).



If $AB = PQ$, $AC = PR$ and $\hat{BAC} = \hat{QPR}$, then $\triangle ABC$ is congruent to $\triangle PQR$ (SAS Congruence Test).

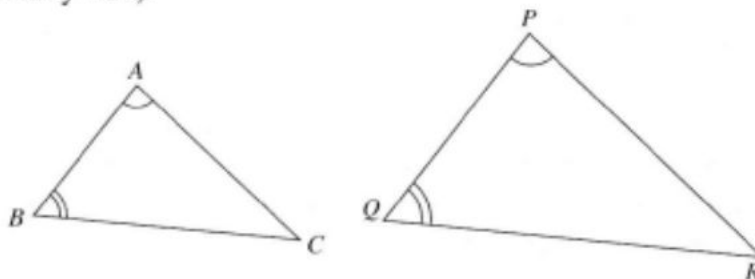


If $AC = XZ$, $AB = XY$ or $BC = YZ$, and $\hat{ABC} = \hat{XYZ} = 90^\circ$, then $\triangle ABC$ is congruent to $\triangle XYZ$ (RHS Congruence Test).

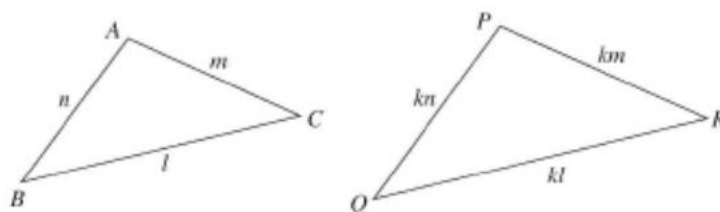


Similar Triangles

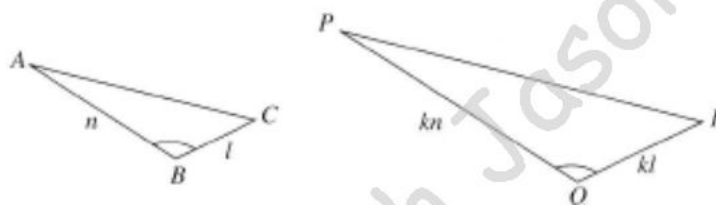
If $\hat{BAC} = \hat{QPR}$ and $\hat{ABC} = \hat{PQR}$, then $\triangle ABC$ is similar to $\triangle PQR$ (AA Similarity Test).



If $\frac{PQ}{AB} = \frac{QR}{BC} = \frac{RP}{CA}$, then $\triangle ABC$ is similar to $\triangle PQR$ (SSS Similarity Test).



If $\frac{PQ}{AB} = \frac{QR}{BC}$ and $\angle B = \angle Q$, then $\triangle ABC$ is similar to $\triangle PQR$ (SAS Similarity Test).



Probability

$$\text{Probability} = \frac{\text{Number Of Successful Outcome}}{\text{Total Number Of Outcomes}}$$

If the probability of **A AND B** occurs, then $P(A) \times P(B)$.

If the probability of **A OR B** occurs, then $P(A) + P(B)$

If the probability of **A DOES NOT** occurring, then $1 - P(A)$.

Probability is between and include 0 to 1.

If Probability (P) = 0, it means that there is **NO CHANCE** of success.

If Probability (P) = 1 it means that success is **CERTAIN**.

Statistics

Ungroup Data

$$\text{Mean}(\bar{X}) = \frac{\text{Sum Of All Data Values}}{\text{Number Of Data}}$$

Group Data

$$\text{Mean}(\bar{X}) = \frac{\sum fx}{\sum f}$$

$$\text{Lower Quartile} = \frac{1}{4}(n + 1)\text{th Term}$$

$$\text{Median} = \left(\frac{n+1}{2}\right)\text{th Term}$$

$$\text{Upper Quartile} = \frac{3}{4}(n + 1)\text{th Term}$$

n is the total frequency.

*These formulas give the POSITION where the value is located. It IS NOT the actual value.

Ungroup Data - Standard Deviation (σ)

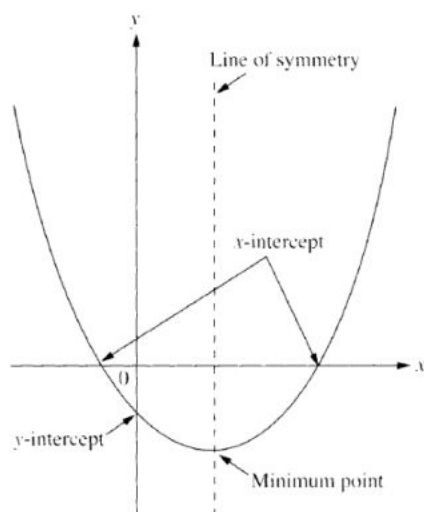
$$\sigma = \sqrt{\frac{\sum (x - \bar{X})^2}{\sum f}} \quad \text{or} \quad \sigma = \sqrt{\frac{\sum x^2}{n} - \bar{X}^2}$$

Group Data - Standard Deviation (σ)

$$\sigma = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2} \quad \text{or} \quad \sigma = \sqrt{\frac{\sum fx^2}{\sum f} - (\bar{X})^2}$$

Graphs

$a > 0$



$a < 0$

